

# Norm-Based Joint Transmit/Receive Antenna Selection (NBJTRAS) Aided and Two-Tier Channel Estimation (TTCE) Assisted STSK Systems

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# Outline

- 1 Introduction
  - Motivation
- 2 NBJTRAS and TTCE
  - NBJTRAS aided STSK systems
  - TTCE for NBJTRAS aided STSK systems
- 3 Simulation Example
  - Simulation Settings
  - Simulation Results
- 4 Conclusions
  - Concluding Remarks

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# Background

- MIMO systems' promise **wonderland** of **diversity** and/or **multiplexing** gains
  - requires **multiple** RF chains, which may lead to a **high power consumption** and **hardware costs**
- **Antenna Selection (AS):**
  - Offers a low-cost technique of **reducing** the number of RF chains utilised at the transmitter and/or receiver, while **retaining** the significant advantages of MIMO systems
- **Challenges:**
  - **Low-complexity** AS is always desirable
  - **Efficient channel estimation (CE)** is needed

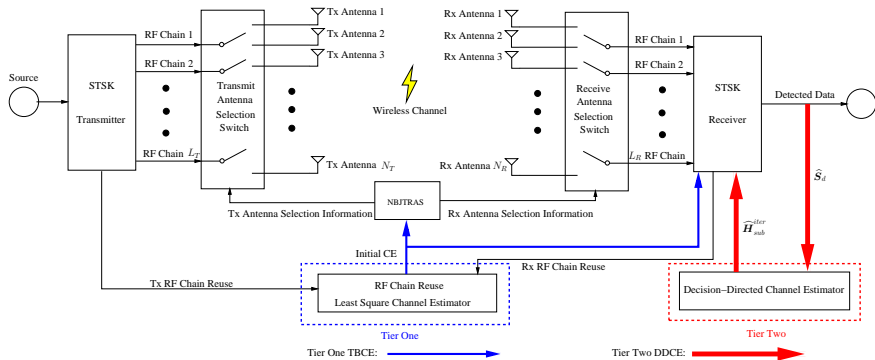
# Our Contributions

- Existing joint transmit/receive AS and CE schemes
  - ① Full-search based AS achieves optimal performance, while imposing a **high complexity**
  - ② Sub-optimal AS leads to a certain **performance loss**
  - ③ Conventional training based CE (TBCE) imposes a **high overhead** required for acquiring accurate CSI, while pure blind CE imposes a **high complexity** and **estimation ambiguities**
- Our novel **NBJTRAS** and **TTCE**
  - ① The new NBJTRAS relies on norm-based antenna selection **optimization** at a much **lower complexity**
  - ② Simple yet efficient TTCE is capable of acquiring **accurate CSI**, while imposing a **low overhead**.

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# Structure of NBJTRAS aided STSK



# Norm-Based Selection (NBS) Criterion

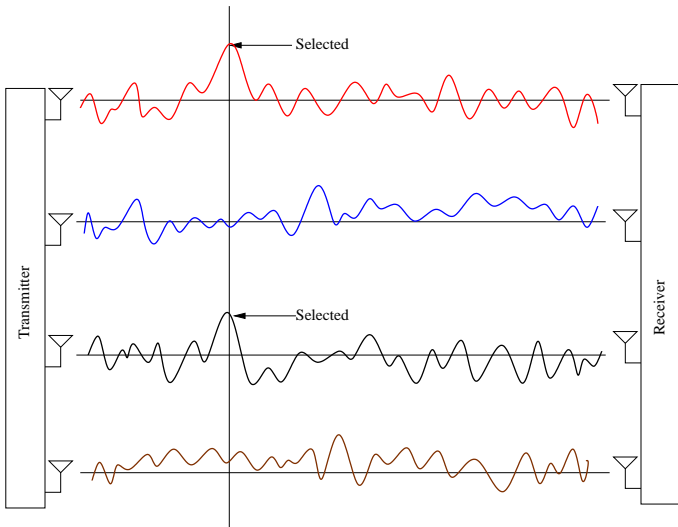
- Let  $\hat{\mathbf{H}}_{sub} \in \mathbb{C}^{L_R \times L_T}$  be the subset candidates of the full channel matrix  $\mathbf{H} \in \mathbb{C}^{N_R \times N_T}$ , while the corresponding selected subset  $\mathbf{H}_{sub}$  based on the NBS criterion may be formulated as:

$$\mathbf{H}_{sub} = \arg \max_{\hat{\mathbf{H}}_{sub} \in \mathbf{H}} \left\{ \sum_{n_t=1}^{L_T} \sum_{n_r=1}^{L_R} \|\hat{\mathbf{H}}_{sub}(n_r, n_t)\| \right\} \quad (1)$$

- Solving the above optimization problem by exhaustive search requires us to evaluate the norms of the  $\mathbb{C}_{N_R}^{L_R} \times \mathbb{C}_{N_T}^{L_T}$  candidate subset matrices, where  $\mathbb{C}_{N_R}^{L_R}$  and  $\mathbb{C}_{N_T}^{L_T}$  are the row-dimension and column-dimension combinations of  $\mathbf{H}_{sub}$ , respectively.



# Norm-Based Selection (NBS) Criterion



# NBJTRAS Algorithm Description

- Given the full channel matrix  $\mathbf{H} \in \mathbb{C}^{N_R \times N_T}$ , without loss of generality, assume  $C_{N_R}^{L_R} < C_{N_T}^{L_T}$ . The NBJTRAS algorithm accomplishes the optimization in **two Steps**:
- Step 1**: Row Based Operations

Let  $i_r \in \{1, 2, \dots, C_{N_R}^{L_R}\}$  be the row combination index, and get the sub-matrix  $\mathbf{H}_{i_r} \in \mathbb{C}^{L_R \times N_T}$ . Compute the magnitude of each column in  $\mathbf{H}_{i_r}$ , which yields the norm metric vector of

$$\mathbf{m}_{i_r}^T = [m_{i_r}^1 \ m_{i_r}^2 \ \dots \ m_{i_r}^{N_T}]. \quad (2)$$

Applying (2) to all the  $C_{N_R}^{L_R}$  possible combinations leads to the norm metric matrix  $\mathbf{M}^T = [\mathbf{m}_1, \mathbf{m}_2, \dots, \mathbf{m}_{C_{N_R}^{L_R}}] \in \mathbb{C}^{N_T \times C_{N_R}^{L_R}}$ .

# NBJTRAS Algorithm Description

- **Step 2:** Column Based Operations

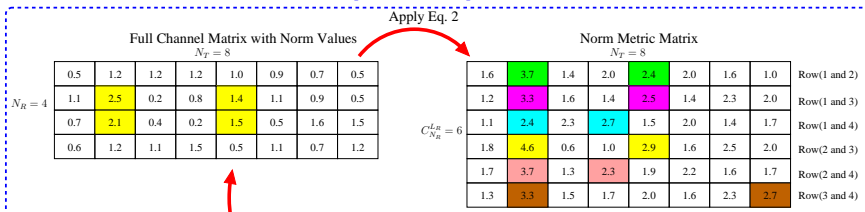
Find the largest  $L_T$  elements in the  $i_r$ th row of  $\mathbf{M}$  and sum them up, which is denoted as  $m_{\max}^{i_r}$ , as well as record the column indices of these  $L_T$  elements in the index vector, producing the max-norm metric vector of

$$\mathbf{m}_{\max}^T = \left[ m_{\max}^1 \quad m_{\max}^2 \quad \cdots \quad m_{\max}^{C_{NR}^{LR}} \right]. \quad (3)$$

Then the optimal sub-set may be found by identifying the largest element in (3).

# An Example of NBJTRAS with $L_T = L_R = 2$

## Step 1: Row Based Operations



Map wining combination  
back to full channel matrix

Wining combination →

6.1
5.8
5.1
7.5
6.0
6.0

3.7	2.4
3.3	2.5
2.4	2.7
4.6	2.9
3.7	2.3
3.3	2.7

Find  $L_T = 2$   
largest elements  
of each combination

Sum up elements in each combination

## Step 2: Column Based Operations

# Complexity Comparison

- Complexity of the **Exhaustive Search**:

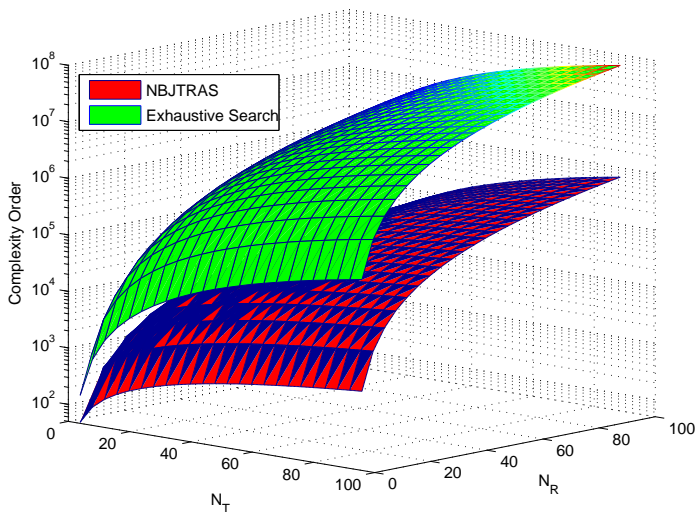
$$C_{ES} \approx \mathcal{O} \left( (L_R \cdot L_T) \cdot \left( C_{N_T}^{L_T} \cdot C_{N_R}^{L_R} \right) \right)$$

- Complexity of the **NBJTRAS**:

$$C_{NBJTRAS} \approx \mathcal{O} \left( (N_T \cdot L_R) \cdot C_{N_R}^{L_R} \right) \text{ (if } C_{N_R}^{L_R} \leq C_{N_T}^{L_T} \text{)}$$

$$\text{or } C_{NBJTRAS} \approx \mathcal{O} \left( (N_R \cdot L_T) \cdot C_{N_T}^{L_T} \right) \text{ (if } C_{N_R}^{L_R} > C_{N_T}^{L_T} \text{)}$$

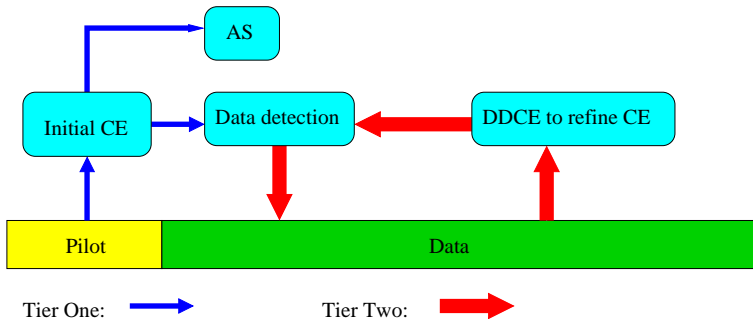
# Complexity Comparison Figure



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# Structure of Two-Tier Channel Estimation for NBJTRAS





# Two-Tier Channel Estimation for NBJTRAS

- **Tier One:** Training Based CE (**TBCE**) for AS
  - We adopt the **low-complexity** TBCE relying on a low training overhead in **Tier One** to maintain a **high throughput** at the cost of a **poor CE**
  - AS is relatively **insensitive** to CE errors, therefore this inaccurate CE is adequate for the NBJTRAS scheme
  - The RF chains are **reused** during the estimation of the full channel matrix.
- **Tier Two:** Decision-Directed CE (**DDCE**) for data detection
  - Data detection requires **accurate** CE
  - Semi-blind DDCE employs detected data for further **refining** CE quality

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# Simulation Settings

- 1 Quasi-static Rayleigh fading MIMO:  
STSK( $L_T = 2, L_R = 2, T_n = 2, Q = 4, 4QAM$ )
- 2 AS factor is defined as  $f_{AS}(N_T, N_R) = \frac{N_T + N_R}{L_T + L_R}$
- 3 Transmitted signal power normalised to unity, SNR defined as  $\frac{1}{N_0}$
- 4 Frame length set to 1,000 bits, yielding  $\tau = 250$  STSK symbol blocks
- 5 Mean Channel Error (MCE):  

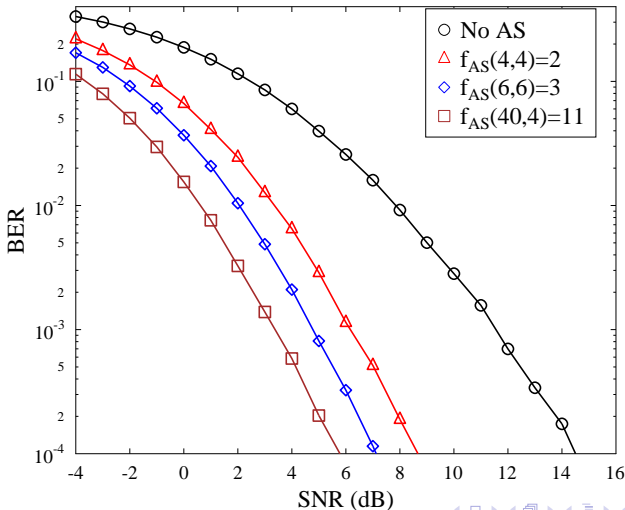
$$J_{\text{MCE}}(\hat{\mathbf{H}}_{\text{sub}}) = \|\mathbf{H}_{\text{sub}} - \hat{\mathbf{H}}_{\text{sub}}\|^2 / \|\mathbf{H}_{\text{sub}}\|^2$$
- 6 All the results were averaged over 10,000 channel realisations

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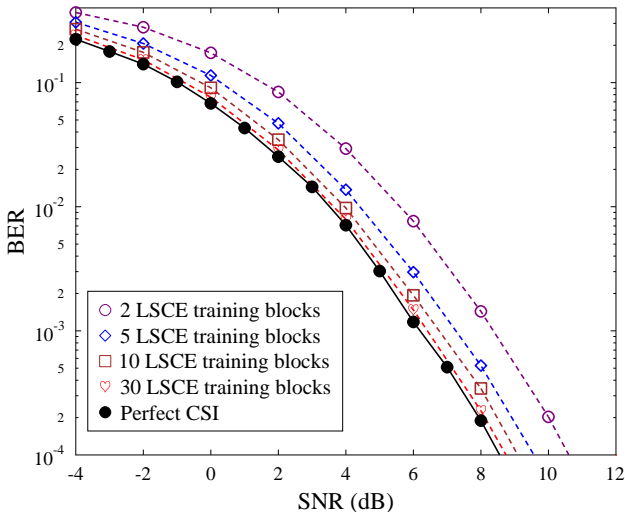
# NBJTRAS Aided STSK with Perfect CSI

- BER performance of the proposed NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) given three AS factors  $f_{AS}(N_T, N_R)$ , in comparison to the performance of the conventional STSK(2, 2, 2, 4, 4QAM) without AS



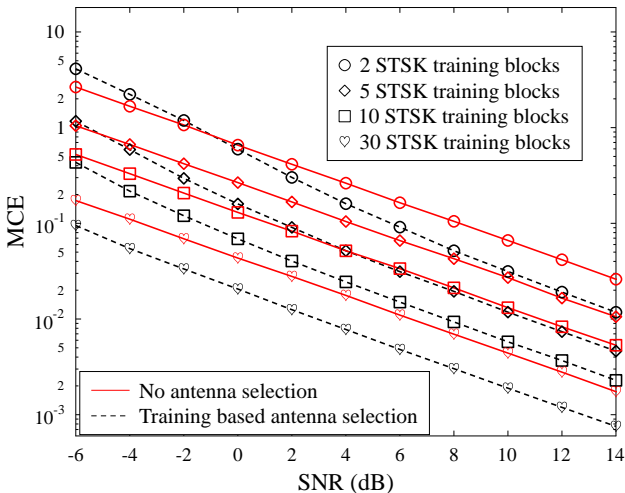
# BER of TBCE for NBJTRAS Aided STSK

- BER performance of the NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $f_{AS}(4, 4) = 2$ , assisted by the conventional TBCE scheme given the number of the STSK training blocks  $M_T = 2, 5, 10$  and 30, in comparison to the perfect CSI case



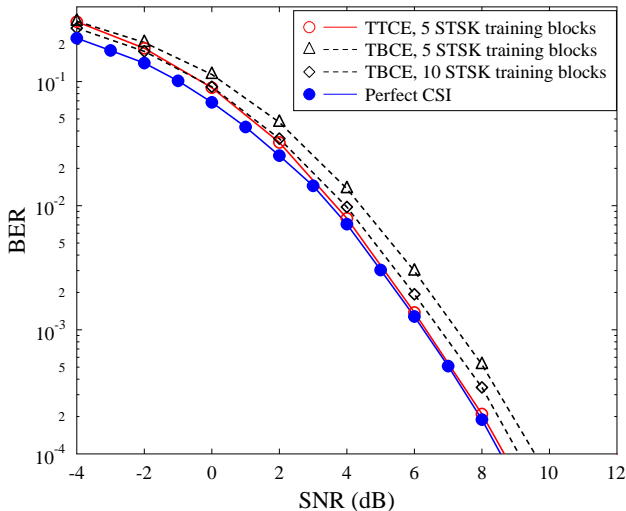
# MCE of TBCE for NBJTRAS Aided STSK

- MCE** performance of the NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $f_{AS}(4, 4) = 2$  and employing the conventional TBCE scheme, in comparison to the performance of the TBCE aided conventional STSK(2, 2, 2, 4, 4QAM) without AS



# BER of TTCE for NBJTRAS Aided STSK

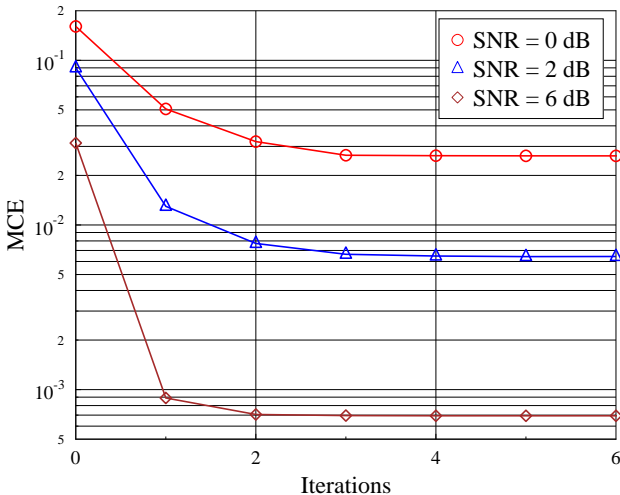
- BER performance of the proposed TTCE based NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $M_T = 5$  initial training blocks, in comparison to that of the conventional TBCE assisted NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $M_T = 5$  and 10.  $f_{AS}(4, 4) = 2$  is adopted for both systems





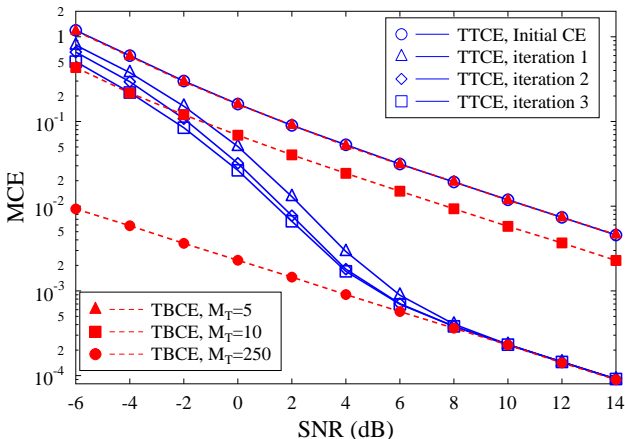
# MCE Convergence Performance of TTCE

- MCE convergence** performance of the proposed TTCE for the NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $f_{AS}(4, 4) = 2$  and  $M_T = 5$  for three SNR values.



# MCE Performance of TTCE

- **MCE** performance of the proposed TTCE for the NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $M_T = 5$ , in comparison to that of the conventional TBCE scheme for the NBJTRAS aided STSK(2, 2, 2, 4, 4QAM) with  $M_T = 5, 10$  and 250.  $f_{AS}(4, 4) = 2$  is adopted for both systems



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# Summary

- We have proposed a simple yet efficient NBJTRAS aided STSK system
  - ① Provides a low-complexity technique of reducing the number of RF chains required by MIMO systems, while retaining the MIMO advantages
  - ② Our NBJTRAS is capable of solving the optimal NBS criterion at a lower complexity compared to the exhaustive search
- We have proposed a novel TTCE scheme for assisting the NBJTRAS aided STSK system
  - ① Only requires a low training overhead in Tier One for AS
  - ② Estimation of the selected sub-channel-matrix is further refined in Tier Two for data detection

**Thank you.**